

This is the accepted version of the following article:

Sun, L., Ji, X., Zhuang, Y. et al. Nonlinear modeling of the ten-story RC building structure of 2015 E-Defense shaking table tests. Bull Earthquake Eng (2023). <https://doi.org/10.1007/s10518-022-01611-9>.

which has been published in final form at [[Link to final article](#)]

# Nonlinear modeling of the ten-story RC building structure of 2015 E-Defense shaking table tests

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## Abstract

In 2015, a full-scale ten-story reinforced concrete (RC) building structure was tested on the E-Defense shake table, the recorded test data from which provided a unique benchmark case to validate a state-of-the-art modeling approach. This paper presents the development and validation of a finite element model of the test building structure established on the OpenSees platform. In this model, RC beams and columns were simulated using the fiber-based beam-column element, and shear walls were modeled with the multi-layer shell element. The numerical model provided a reasonable estimate of the observed global responses of the test structure, including peak inter-story drifts and floor accelerations, for the wall direction. The multi-layer shell element effectively tracked the local strain, flexural and shear deformations of RC walls. Although the numerical model reasonably captured responses for the frame direction under base fixed JMA-Kobe 50% shaking, the simulation of RC frames was less accurate for base fixed JMA-Kobe 100% shaking when the test structure experienced significant damage at the maximum inter-story drift of 2.9%. Finally, a couple of important modeling issues for RC structure were discussed, including beam-column joint modeling and damping modeling. Use of the scissors model to represent the beam-column joints led to an improved estimation of the inter-story drifts of stories where the beam-to-column joints experienced severe damage. A transient Rayleigh damping model, in which a tangent stiffness matrix was used to formulate a system damping matrix, was recommended for structural nonlinear response history analysis.

**Keywords:** reinforced concrete (RC) structure; E-Defense shaking table test; nonlinear response history analysis; RC wall modeling; beam-column joint modeling.

## 1 Introduction

Tall buildings are widely constructed in modern cities around the world. Currently, the performance-based design has been merged as an alternative to the traditional prescriptive strength-based design for tall buildings (Moehle 2008). In the performance-based seismic design framework, nonlinear response history analysis of the structural model subjected to a suite of ground motions is commonly adopted to predict building responses at varying levels of seismic intensity. Afterwards, the estimated seismic responses are compared with the acceptance criteria defined as per the target performance levels. Therefore, accurate and reliable numerical models are crucial in the implementation of the performance-based design and assessment.

In past decades, significant efforts have been made in development of numerical modeling approaches of reinforced concrete (RC) building structures. Beam-column element with hinges (Powell and Chen 1986) and fiber beam-column element (Spacone et al. 1996) are two commonly-used modeling approaches for RC beams or columns. In the former approach, the concentrated hinges are required to be defined by the phenomenological description of the overall force-deformation relationship of the component, while the latter approach calculates the force-displacement response of the component by implicit integration of flexural stresses and strains through the cross section and along the member with predefined stress-strain relationships of materials. Various conceptually different models have been developed to model

41 RC shear walls, such as the Multiple-Vertical-Line-Element-Model (MVLEM) (Orakcal et al. 2004, Kolozvari et al. 2021a),  
42 Shear-Flexure-Interaction Multiple-Vertical-Line-Element-Model (SFI-MVLEM) (Kolozvari et al. 2015, 2021b), multi-  
43 layer shell element model (Lu et al. 2015a), and beam-truss model (Lu and Panagiotou 2014). Due to a high level of  
44 numerical stability, the MVLEM and multi-layer shell element models are often used in structural nonlinear analysis.  
45 Scissors model (Alath and Kunnath 1995) has been developed to represent the RC beam-to-column joints, and it is often  
46 adopted in nonlinear response history analysis of building structures due to its computational efficiency. PEER/ATC 72-1  
47 presents a compilation of the numerical modeling approaches of the structural components and systems (PEER/ATC 2010).

48 Currently available research which is used as a basis to justify the modeling approaches of RC structures is almost  
49 exclusively based on experimental tests of individual structural components and relative small-scale substructures. As  
50 large-scale shaking table tests on RC building structure systems are very limited except for a few (e.g., full-scale four-story  
51 structure tests in E-Defense (Gavridou et al. 2017), seven-story RC wall structure tests in UCSD (Moaveni et al. 2011)),  
52 the modeling approaches have not been well validated against the structural system-level test data. It is a clear need to  
53 conduct large-scale dynamic tests of RC tall building structures, and validate state-of-the-art modeling approaches using  
54 the experimental data.

55 In 2015, E-Defense conducted shaking table tests of a full-scale ten-story reinforced concrete (RC) structure, which was  
56 heavily instrumented to record the global and local responses of the test structure under various levels of seismic shaking  
57 (Kajiwara et al. 2021). The objective of this study is to validate state-of-the-art numerical models using the valuable test  
58 as a unique benchmark case, which would provide us an insight on how accurate current modeling approach is in simulating  
59 the nonlinear response responses of RC building structures. The next section presents an overview of E-Defense shaking  
60 table tests in 2015. In the third section, the modeling approach of the test structure is described in detail. The simulation  
61 results are presented in the fourth section. Finally, a couple of important modeling issues, i.e., beam-column joint modeling  
62 and damping modeling, are discussed in the fifth section.

## 63 **2 Overview of E-Defense shaking table tests**

### 64 **2.1 Test structure and loading protocol**

65 To obtain realistic seismic responses of high-rise buildings with sliding bases or with fixed bases, a full-scale ten-story  
66 reinforced concrete (RC) building was tested on the E-Defense shake table in 2015 using three-directional seismic motion  
67 inputs (Fig. 1) (Kajiwara et al. 2021). The test specimen had a plan dimension of 13.5 m × 9.5 m, and the total height of  
68 the ten stories was 25.75 m. The test structure comprised RC frames in the longitudinal direction (hereinafter referred to  
69 as the frame direction), and adopted the frame-wall interacting system in the transverse direction (hereinafter referred to as  
70 the wall direction) where the RC shear walls were assigned from the 1<sup>st</sup> to 7<sup>th</sup> stories.

71 Two sets of experiments were conducted on the test structure. First, the structure was able to move sideways with a base  
72 sliding mechanism. Cast-iron plates were placed at the bottom of the foundation base to generate a low friction coefficient  
73 (0.2-0.25) (Enokida et al. 2013). Seismic motions including 10%, 25%, 50%, and 100% JMA-Kobe were applied to the  
74 specimen in sequence during the base sliding tests. Next, the foundation beam was fixed on the shaking table and base  
75 fixed tests were conducted. The specimen was subjected to 10%, 25%, 50%, 100%, and 60% JMA-Kobe in sequence.  
76 Before and after each seismic motion shaking, a white-noise excitation was performed for system identification. The  
77 heavily instrumented test structure provided comprehensive data on structural responses, including both global responses  
78 (e.g., inter-story drifts, floor accelerations, etc.) and local responses (e.g., beam/column end rotations, deformations of  
79 beam-column joints, vertical strains of RC walls, etc.). Further details on the specimen design and test results can be found  
80 in Kajiwara et al. (2021).



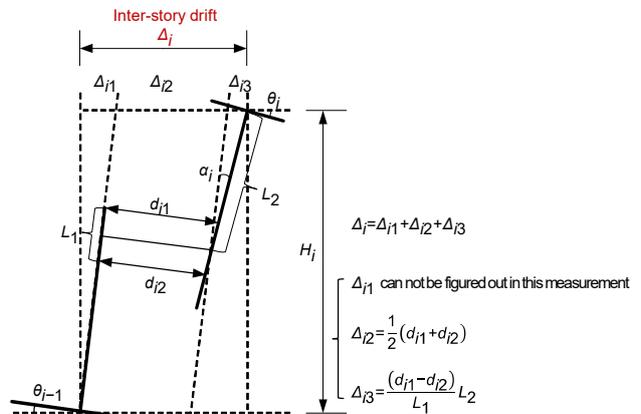
Fig. 1 Photograph of the test structure

81 **2.2 Measurement of inter-story drifts**

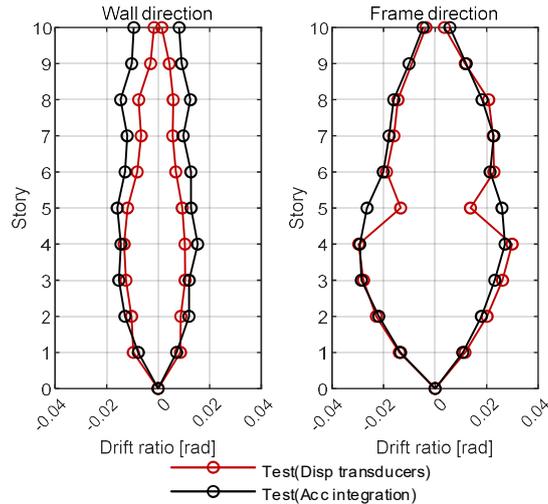
82 In the shaking table tests, displacement transducers were installed in each story as illustrated in Fig. 2a. Inter-story drift  
 83 was obtained by the average value of measured displacements from the upper and lower displacement transducers ( $d_{i1}$  and  
 84  $d_{i2}$  in Fig. 2a) on a supporting column, corresponding to  $\Delta_{i2}$  (as illustrated in Fig. 2a). However, lateral drifts resulting from  
 85 floor slab rotations ( $\Delta_{i1}$  and  $\Delta_{i3}$  in Fig. 2a) were not included in the measurement, which might have led to an  
 86 underestimation of inter-story drifts. Double-integration of floor acceleration data is another approach for the measurement  
 87 of drifts. The floor acceleration measured using accelerometers was firstly band-pass filtered (0.2-30Hz in this study) to  
 88 exclude the effect of noise, and then integrated to obtain the floor velocity. Baseline correction was implemented before  
 89 integrating the velocity to obtain the absolute displacement of each floor. Inter-story drift of each story was calculated from  
 90 the displacement responses of the adjacent floors. Fig. 2b presents the inter-story drift ratios obtained from the two sets of  
 91 measurements under 100% JMA-Kobe shaking in base fixed tests. This indicates that the two methods provided nearly  
 92 identical results in the frame direction except for the fifth-story drift, while the displacement transducer measurement  
 93 provided smaller results than the accelerometer measurement due to the non-negligible floor slab rotation in the wall  
 94 direction. This observation is consistent with that in another shaking table test (Ji et al. 2022), in which the effect of floor  
 95 slab rotation on the inter-story drift measurement was quantified. This discrepancy became more notable at upper stories  
 96 because the lateral deformation in the wall direction was characterized by a flexure type mode and the floor rotation  
 97 gradually increased along the increasing height of floors. Therefore, the inter-story drifts obtained by double-integration of  
 98 acceleration were adopted in the following validation of the numerical simulation.



(a) Displacement transducer arrangement



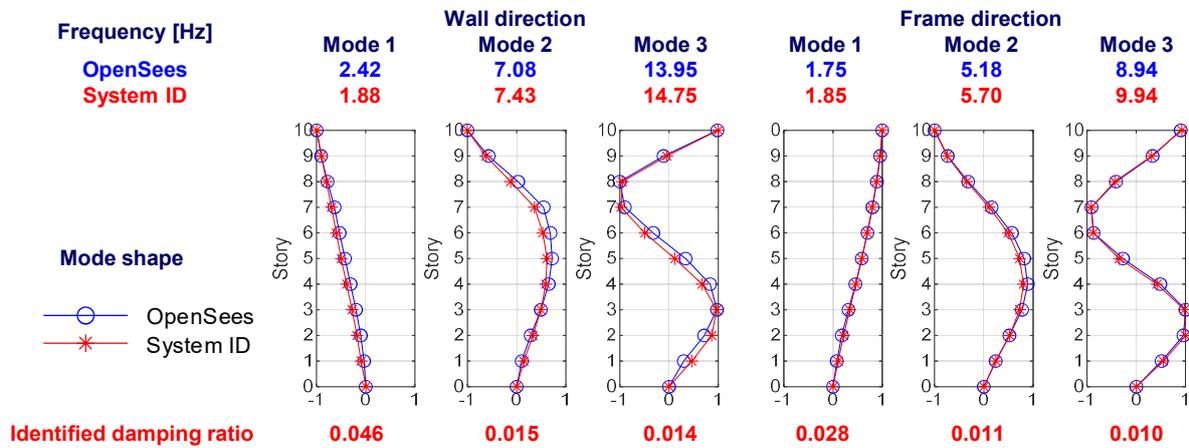
(b) Decomposition of measured inter-story drifts



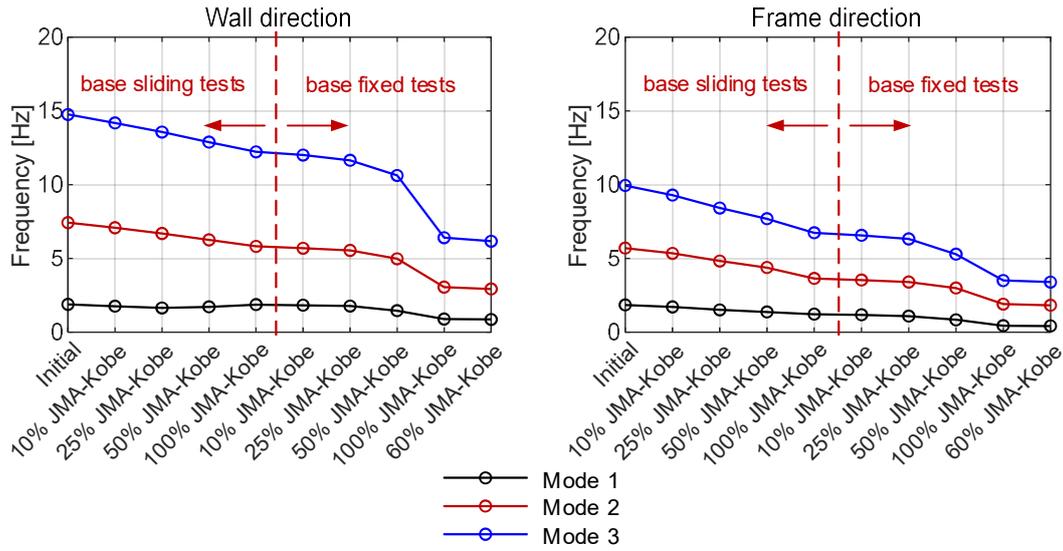
(c) Comparison between two measurements  
Fig. 2 Measurements of inter-story drifts

99 **2.3 System identification**

100 Dynamic properties of the test structure before and after each level of seismic motion shaking were identified using the  
 101 autoregressive with exogenous terms (ARX) method (Ji et al. 2011) from white noise test data. Fig. 3a depicts the identified  
 102 natural vibration frequencies, damping ratios and mode shapes of the first three modes in the wall and frame directions of  
 103 the undamaged test structure. Fig. 3b indicates that the first three translational modal frequencies decreased gradually after  
 104 increasing levels of seismic motion shakings. After all seismic loads, the 1<sup>st</sup> modal frequency decreased by 54% in the wall  
 105 direction and 77% in the frame direction, indicating severe damage and stiffness degradation of the test structure.



(a) Dynamic properties of the undamaged test structure



(b) Identified modal frequencies after each shaking  
Fig. 3 System identification results

### 106 3 Numerical modeling approach

107 A numerical model was established in the structural analysis platform OpenSees (McKenna et al. 2000) according to the  
108 measured material properties and geometrical dimensions of the shaking table test structure. This section describes the  
109 details of the numerical model of the test structure.

#### 110 3.1 Material modeling

111 The Kent-Park model (Kent and Park 1971) was adopted to define the compressive uniaxial stress-strain curve of  
112 unconfined concrete, which consists of a parabolic ascending branch and a linear descending branch. The peak stress  $f'_c$   
113 was obtained from concrete cylinder tests, and the peak strain  $\epsilon_{c0}$  was assumed to be 0.002. Elastic modulus  $E_{c0}$  was defined  
114 as  $2f'_c/\epsilon_{c0}$  in this model. The stirrup-confined concrete was represented by the Saatcioglu-Razvi model (Saatcioglu and  
115 Razvi 1992), which takes into account the increase of strength and ductility caused by confining effect. The residual  
116 compressive strength was taken as zero for unconfined concrete and 0.2 times the peak strength for stirrup-confined  
117 concrete. A bilinear stress-strain curve was used to define the envelope of concrete uniaxial tensile behavior. The linear  
118 ascending branch had a slope equal to the elastic modulus of concrete in compression, and the concrete tensile strength  
119 corresponding to cracking was taken as  $f_t = 0.31\sqrt{f'_c}$  (unit in MPa), as suggested by Berlabi and Hsu (1994). The post-  
120 cracking linear descending branch represented the tension stiffening effect of concrete, with a negative slope of 0.05 times  
121 the concrete elastic modulus. It is important to note that the hysteretic behavior of concrete in RC beams and columns  
122 followed the criteria proposed by Yassin 1994 (implemented as *Concrete02* material in OpenSees), while the concrete in  
123 RC walls was modeled with the hysteretic rules of *PlaneStressUserMaterial* (an origin-oriented linear curve was adopted  
124 for the unloading and reloading path), as illustrated in Fig. 4a. For *PlaneStressUserMaterial*, concrete was assumed to  
125 behave in a plane-stress manner, and the cracking of concrete was modeled by the fixed smeared crack approach. When  
126 the principal tensile stress exceeded the specified concrete tensile strength, cracks were assumed to occur, and concrete  
127 was treated as an orthotropic material after cracking. The reduced shear stiffness for post-cracking concrete was taken to  
128 be  $\eta G$ , where  $G$  was the concrete elastic shear modulus and  $\eta$  was the shear retention factor to account for the post-cracking  
129 shear stiffness deterioration. The value of shear retention factor  $\eta$  was recommended to be approximately 0.1 (Ile and  
130 Reynouard 2000, Ji et al. 2015). In this simulation, a value of 0.08 was used for  $\eta$ , as determined by trial and error.

131 As shown in Fig. 4b, the uniaxial behavior of reinforcement was represented by the Giuffr -Menegotto-Pinto model with

132 isotropic strain hardening (Filippou et al. 1983), which was implemented as *Steel02* material in OpenSees. This model has  
 133 been well-calibrated and is capable of capturing the nonlinear hysteretic responses of reinforcement. Yield strength and  
 134 elastic modulus of the reinforcement were determined by tensile tests of steel rebars, and the strain hardening ratio was set  
 135 to be 0.01. The parameters which control the transition from elastic to plastic branches, including  $R_0$ ,  $cR_1$ , and  $cR_2$ , were  
 136 taken as 20, 0.925, and 0.15, respectively.

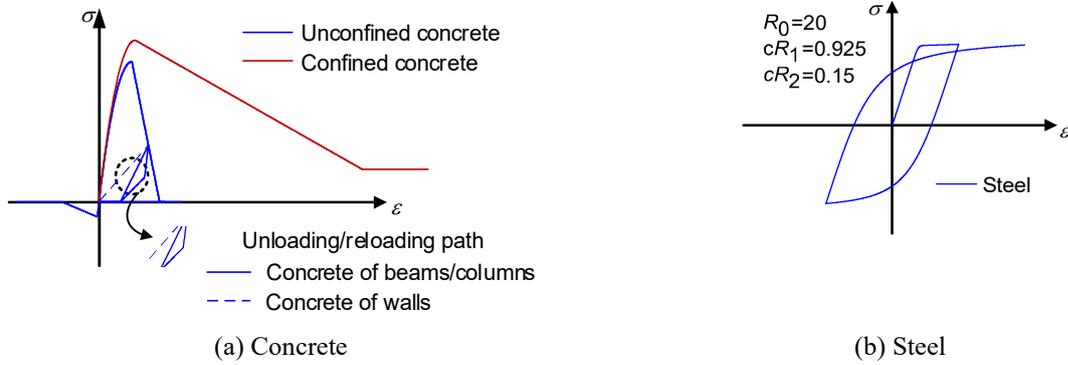
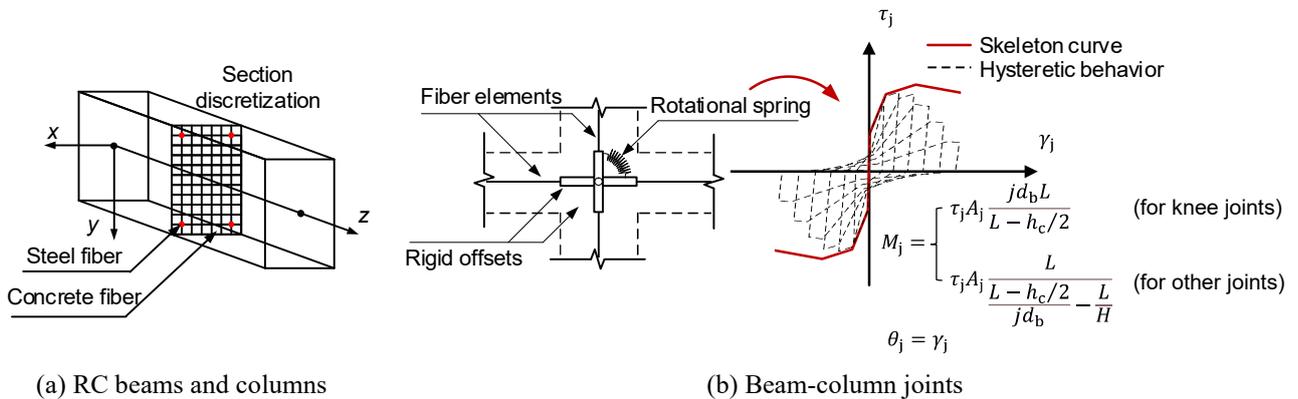


Fig. 4 Uniaxial stress-strain relationship of materials

### 137 3.2 Element modeling

138 Beams and columns in the specimen were modeled by a displacement-based beam-column element (implemented as  
 139 *dispBeamColumn* in OpenSees) with a fiber section (Spacone et al. 1996), as depicted in Fig. 5a. Cover concrete, stirrup-  
 140 confined concrete, and longitudinal rebars in a beam or column were represented by a number of fibers with their  
 141 corresponding uniaxial constitutive relationships. Each beam or column of the test structure was discretized into five  
 142 elements along the longitudinal axis with three integration points. A T-shaped cross-section was adopted for the beams to  
 143 consider the slab effect. The effective overhanging flange widths of beams were determined per the Chinese design code  
 144 for design of concrete structure GB50010-2010 (China Ministry of Housing and Urban-Rural Development 2015), as  
 145 illustrated in Fig. 6. A rigid diaphragm was assigned to constrain all nodes at a floor level. However, this could potentially  
 146 over-constrain the axial deformation of beams, resulting in unrealistic axial forces in beam elements with fiber section and  
 147 overestimation of the strength capacity of the whole structure (Liu et al. 2012). To eliminate the fictitious axial forces, an  
 148 “axial buffer element” (Barbagallo et al. 2020) was added in the beam end to relieve possible over-constraint on the axial  
 149 deformation of beams.



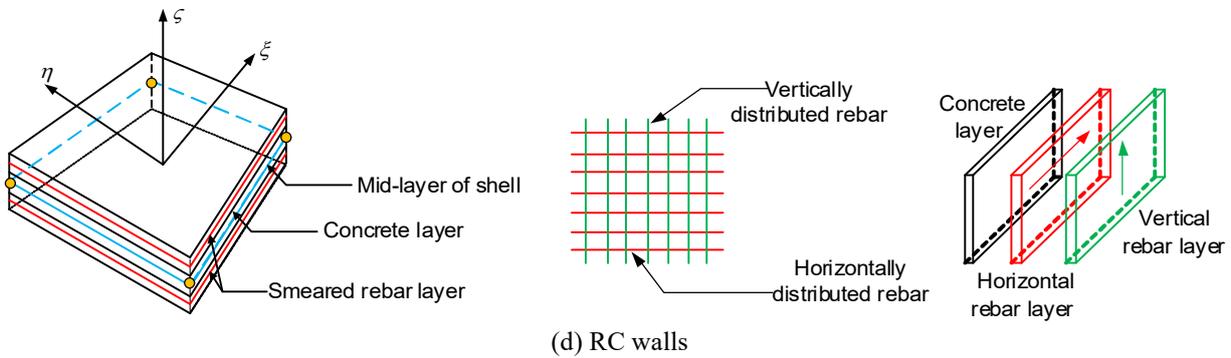
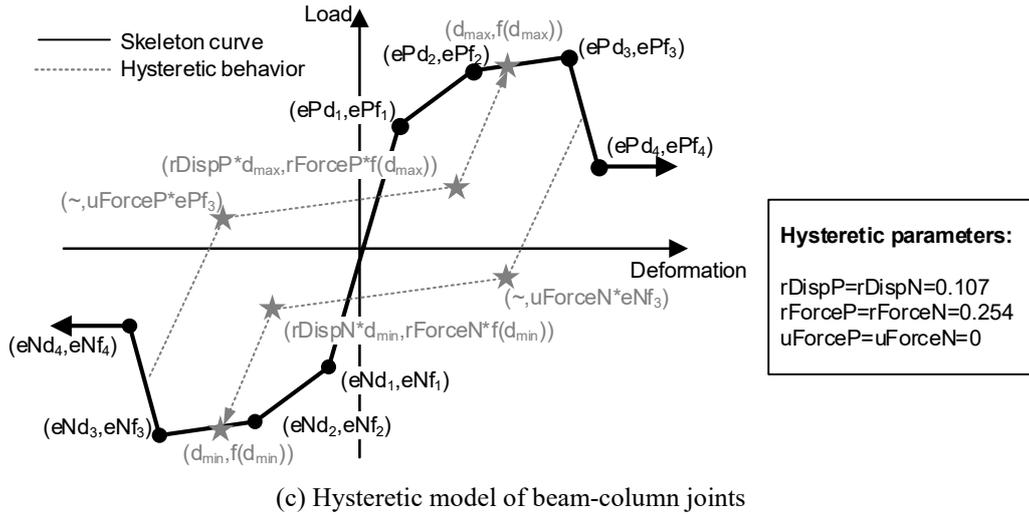
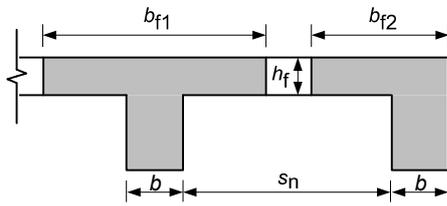


Fig. 5 Element modeling in the simulation



Flange in each side of web:  $b_{f1} = \min\{L_0/3, b+s_n, b+12h_f\}$

Flange in one side of web:  $b_{f2} = \min\{L_0/6, b+s_n/2, b+5h_f\}$

Note:

$b$ : width of beam web

$L_0$ : span length of beam

$s_n$ : clear distance between adjacent beam webs

$h_f$ : thickness of slab

Fig. 6 Effective flange width of T-shaped beam per Chinese code GB50010-2010

150 Beam-column joints were represented with scissors model in both wall and frame directions, as shown in Fig. 5b. In a joint,  
 151 rotational spring was represented by the *zeroLength* element, and the rigid offsets were modeled by *elasticBeamColumn*  
 152 elements with rigid stiffness (using very large Young's modulus of  $3e10$  N/mm<sup>2</sup>). The nonlinear joint shear stress-strain  
 153 ( $\tau_j$ - $\gamma_j$ ) relationship was modeled with the quadrilinear backbone curve proposed by Lafave and Kim (2011). The moment-  
 154 rotation ( $M_j$ - $\theta_j$ ) relationship was obtained using the equations in Fig. 5b (Hassan and Moehle 2012), where  $L$  is the length  
 155 from the beam inflection point to the column centerline, approximated as a half beam centerline span;  $jd_b$  is the beam lever  
 156 arm, which was approximated as 0.90 times the effective beam depth;  $H$  is the column height measured between column  
 157 inflection points, approximated as the story height;  $h_c$  is the height of the column cross-section; and  $A_j$  is the effective joint  
 158 shear area, which is taken as the product of effective joint width (average of beam and column widths) and column depth  
 159 (Kim 2007). *Pinching4* material was adopted to assign the moment-rotation relationship to the joint rotational spring  
 160 (*zeroLength* element). The parameters defining hysteretic responses and their values are illustrated in Fig. 5c, which have  
 161 been calibrated against past test data (Theiss 2005).

162 RC walls in the test structure were modeled by a shell element (implemented as *ShellDKGQ* in OpenSees) with a multi-  
 163 layer shell section (Lu et al. 2015), which can simulate the coupled in-plane and out-of-plane behaviors of RC walls. The

164 multi-layer shell element for modeling structural wall components has been validated to ensure both computational  
165 efficiency and a reasonable level of accuracy (Lu et al. 2013, Ji et al. 2015). It consists of a number of concrete layers and  
166 rebar layers (Fig. 5d). Different layers in the shell element were assumed to be fully bonded in the thickness direction, and  
167 the deformation of each layer was obtained from that of the middle layer based on the plane-section assumption. For the  
168 wall webs, the cover and inside concrete were represented by a number of unconfined concrete layers, and the distributed  
169 reinforcements were represented by the smeared rebar layers in vertical and horizontal directions, respectively. For the  
170 boundary elements, the longitudinal rebars were modeled with truss elements, and the boundary core concrete was  
171 represented by stirrup-confined concrete layers. Each wall at a story was discretized into five by ten meshes in the vertical  
172 and horizontal direction, respectively, and sixteen layers in the thickness direction.

### 173 **3.3 Mass, damping, loading, and boundary conditions**

174 Tributary mass was assigned at the wall and column nodes at each floor level along with the tributary gravity load (dead  
175 and live). Rayleigh damping with a tangent stiffness matrix was adopted for structural damping modeling. Fig. 3a presents  
176 the first three translational modal damping ratios in the wall and frame directions of the test structure at the initial state,  
177 which was identified from the white noise test data. Note that in the system identification, the apparent damping induced  
178 by pitching of shaking table was removed (Molina et al. 2008). In the wall direction, the average damping ratio of the first  
179 three modes was 0.025, and that in the frame direction was 0.016. In addition, ASCE 7-16 (American Society of Civil  
180 Engineers 2016) specifies that the inherent damping of a structure shall not exceed 0.025 equivalent viscous damping in  
181 the significant modes of responses. Therefore, damping coefficients were formulated by setting a damping ratio of 0.025  
182 for the 1<sup>st</sup> and 9<sup>th</sup> structural modes (corresponding to the 1<sup>st</sup> translational mode in the frame direction and 3<sup>rd</sup> translational  
183 mode in the wall direction, respectively). In the calculation of Rayleigh damping coefficients, modal frequencies were  
184 obtained from system identification using white noise test data and updated after each seismic motion shaking.

185 The foundation beams of the test structure were not modeled. All the degrees of freedom (DOF) of nodes at column bases  
186 were fully fixed, and the nodes of wall bottom were pinned at the base. The shaking table test consisted of two phases: the  
187 base sliding phase and base fixed phase. For the nonlinear response history analysis, three-directional acceleration data  
188 measured at the foundation top face of the test specimen were used as the seismic input. Therefore, the sliding behavior of  
189 the foundation was not explicitly simulated. All seismic motion inputs were applied consecutively in the numerical  
190 simulation to reflect the effect of cumulative damage to the test structure. P-Delta effects were considered in the modeling.  
191 Newmark- $\beta$  method and ModifiedNewton algorithm were adopted in the nonlinear response history analysis with  
192 *NormDispIncr* for convergence test. In each loading step, the tolerance for convergence test was 0.001 m and the maximum  
193 number of iterations was 100.

## 194 **4 Numerical simulation results**

195 This section presents comparisons of experimental and analytical responses (e.g., inter-story drift, floor acceleration, base  
196 shear force, overturning moment, and local responses) particularly for base fixed 50% and 100% JMA-Kobe shaking tests,  
197 as the test structure exhibited obvious nonlinear responses in these loading cases.

### 198 **4.1 Dynamic properties**

199 Modal analysis of the numerical model estimated the natural vibration frequencies and associated mode shapes of the test  
200 structure. As shown in Fig. 3a, the dynamic properties of the initial test structure estimated by the numerical model  
201 correlated well with the system identification results, except for some discrepancy in the 1<sup>st</sup> modal frequency of the wall  
202 direction. This discrepancy was because the base sliding foundation was not explicitly simulated in the numerical model.  
203 The test structure was able to move sideways with a base sliding mechanism in the initial state and base uplifting in the

204 wall direction was observed during the white noise test (Tosauchi et al. 2018), while those boundary conditions were not  
 205 considered in the numerical model. Nevertheless, such discrepancy would not influence the nonlinear response simulation  
 206 of base fixed 50% and 100% JMA-Kobe loading cases which is the highlight of the study, as in such loading cases the  
 207 foundation beams were fully anchored on the shaking table.

208 **4.2 Response envelopes**

209 Figs. 7 and 8 depict the peak inter-story drift ratios and peak floor accelerations distributed along the height of the test  
 210 structure when subjected to 50% and 100% JMA-Kobe motions (base fixed tests). As indicated in Fig. 7a, when subjected  
 211 to 50% JMA-Kobe, the calculated peak drift values and their distribution along the structural height aligned well with the  
 212 test data in the frame direction, while somewhat discrepancy is found in the wall direction. The average error of the  
 213 numerical results relative to the test data was 17.5% and 17.0% for the peak floor acceleration in the wall and frame  
 214 direction, respectively, as shown in Fig. 8a. The numerical model is able to capture global seismic responses with  
 215 reasonable accuracy when the structure is in a moderate nonlinear state. Under 100% JMA-Kobe motion, the numerical  
 216 model was still able to provide a reasonable estimate of the inter-story drifts and floor accelerations of the structure in the  
 217 wall direction (see Fig. 7b and Fig. 8b). However, the discrepancy between the numerical simulation and test data became  
 218 notable for the frame direction, with the average errors of the peak inter-story drifts and floor accelerations for all floors  
 219 increasing to 41.1% and 34.4%, respectively. The increased errors in severe nonlinear states (the maximum inter-story drift  
 220 ratio reaching 2.9%) might be due to the modeling of floor slab contribution. In this model, slab contribution was considered  
 221 by T-shaped cross-section beams, and the effective overhanging flange width of each beam was taken as a fixed value per  
 222 the Chinese design code for design of concrete structure GB 50010-2010 (China Ministry of Housing and Urban-Rural  
 223 Development 2015). However, it was revealed that effective overhanging flange widths of beams would change under  
 224 different inter-story drifts (Ning et al. 2014). In addition, Fig. 7b indicates that although the numerical simulation could  
 225 accurately predict the maximum inter-story drift in the 4<sup>th</sup> story, this resulted in an overly concentrated drift distribution  
 226 and an underestimate of the inter-story drift at upper stories. This discrepancy is related to the beam-to-column joint  
 227 modeling, and will be discussed in section 5.1.

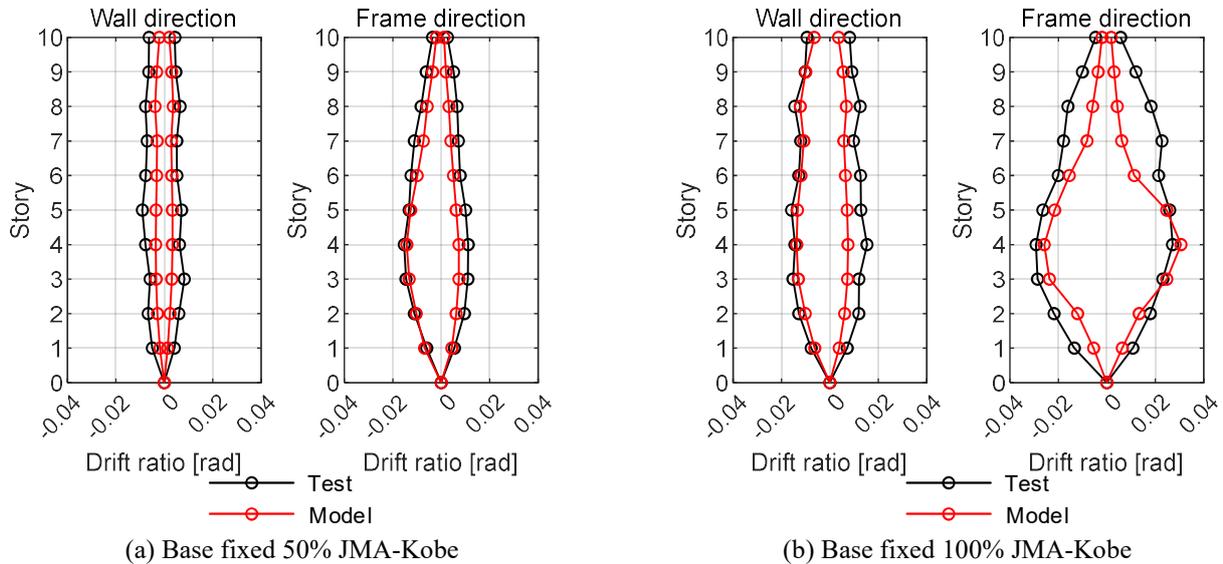
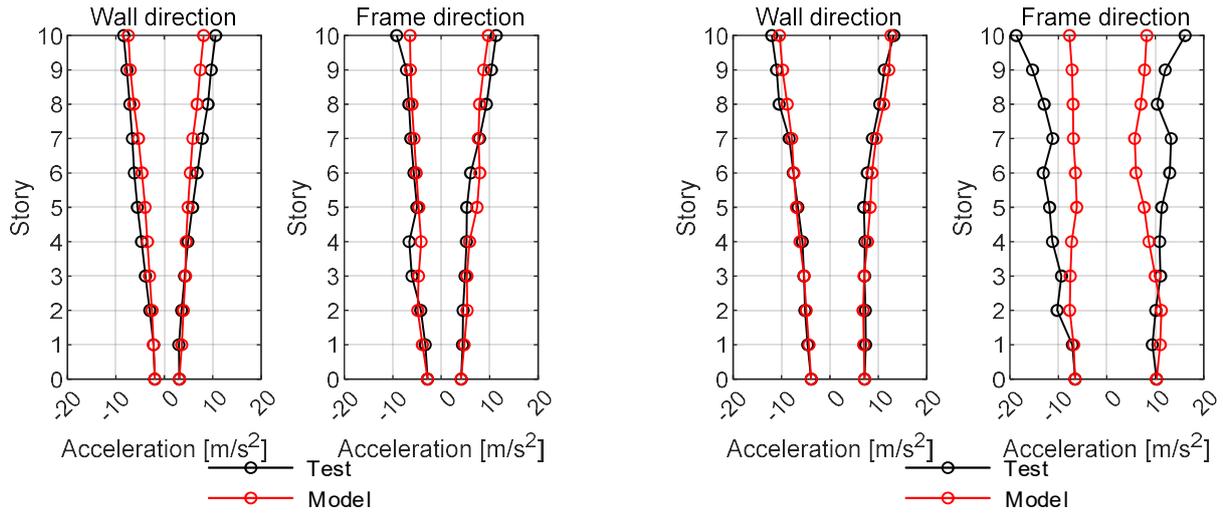


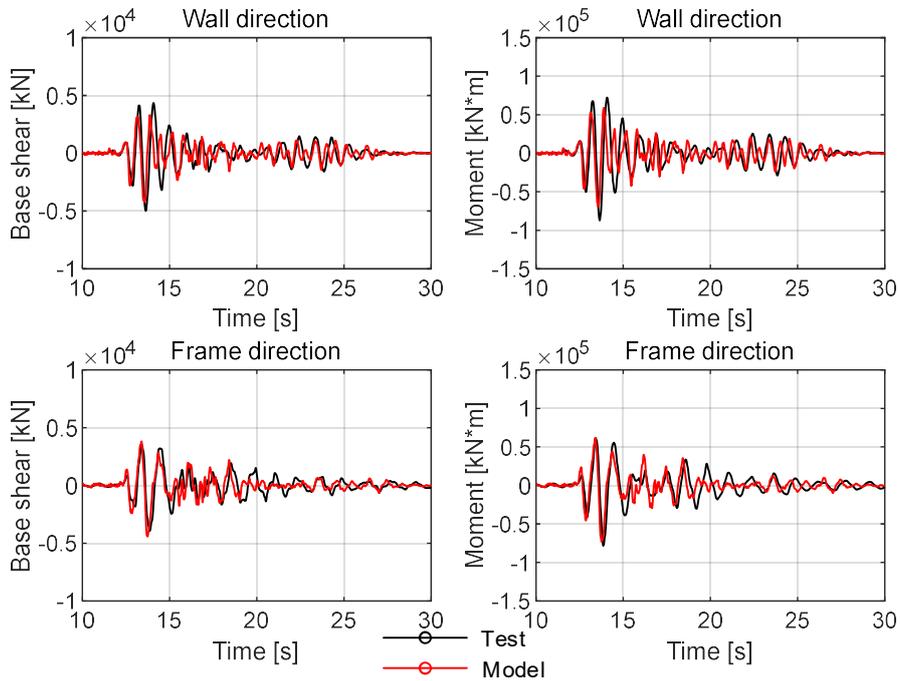
Fig. 7 Inter-story drift ratios along the specimen height



(a) Base fixed 50% JMA-Kobe (b) Base fixed 100% JMA-Kobe  
 Fig. 8 Floor accelerations along the specimen height

229 **4.3 Base shear force and overturning moment**

230 Fig. 9 compares the numerical results and test data for the base shear force and overturning moment of the test structure. It  
 231 is important to note that the values were calculated from the measured/calculated floor accelerations, floor masses and floor  
 232 heights. The numerical model reasonably tracked the base shear force and overturning moment responses with the test  
 233 results, for both 50% and 100% JMA-Kobe loadings.



(a) Base fixed 50% JMA-Kobe

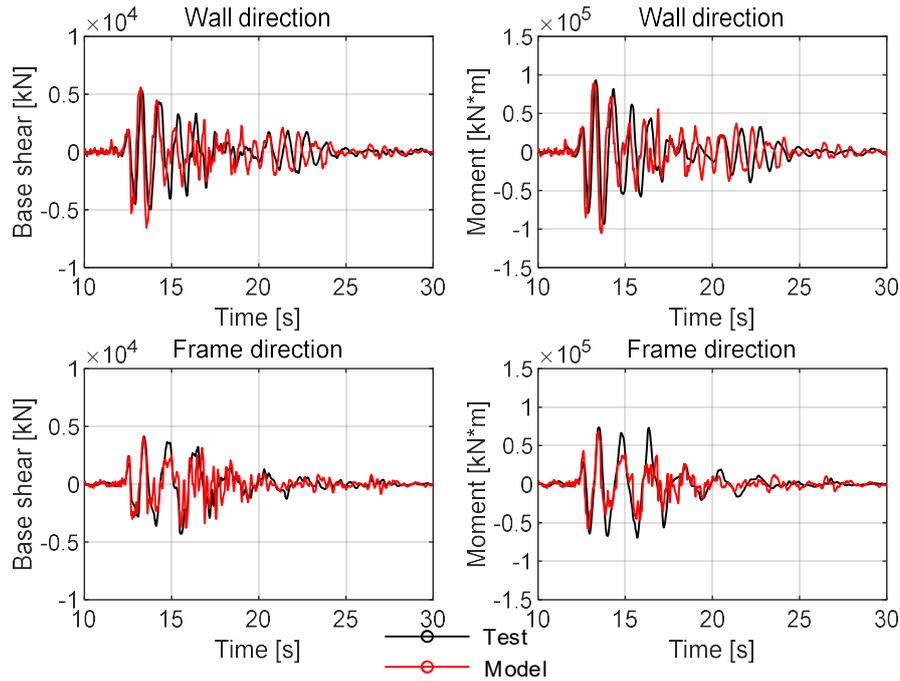


Fig. 9 Base shear force and overturning moment history responses

234 **4.4 Local behavior of RC walls**

235 The capability of the multi-layer shell element to capture the local behavior of RC walls in the test structure was also  
 236 assessed. Using the measured data of the displacement transducers (as shown in Fig. 10), the average vertical strains along  
 237 the wall edges were obtained and the flexural and shear deformation contributions were calculated (Massone and Wallace  
 238 2004). Note that local responses of RC walls were only measured on the bottom three stories. Fig. 11a demonstrates that  
 239 the numerical model accurately captured the boundary vertical strains, flexural and shear deformations in the bottom three  
 240 stories for 50% JMA-Kobe loading. Under 100% JMA-Kobe loading, the numerical model also reasonably captured the  
 241 flexural and shear deformation of RC walls. The experimental data indicated that shear deformation contributed 28.9% to  
 242 the lateral drift of the 1<sup>st</sup>-story wall, and the numerical simulation estimated 20.5% contribution of shear deformation to  
 243 the drift. The wall's boundary vertical strains were estimated with good accuracy in the 1<sup>st</sup> (upper part), 2<sup>nd</sup> and 3<sup>rd</sup> stories.  
 244 However, a notable discrepancy was evident in the lower part (approximately 0.2 times the wall sectional depth) the 1<sup>st</sup>-  
 245 story wall, where the measured tensile strains were significantly larger than the estimated results (see Fig. 11b). This  
 246 discrepancy was because the bottom vertical displacement transducers were end to the foundation beam (see Fig. 10), such  
 247 that the cracks developed at the wall-foundation beam interface would lead to the increase of measured average tensile  
 248 strain. However, the numerical model did not simulate the wall-foundation beam interface behavior.

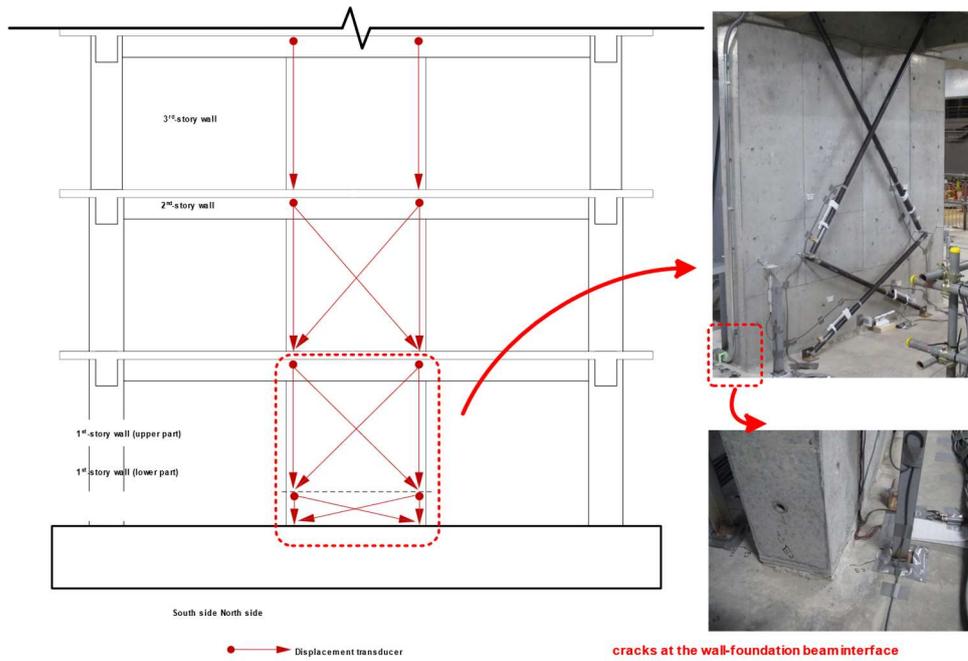


Fig. 10 Displacement transducers on RC walls

Vertical strains  
(at the north side of walls)

Response envelopes

Vertical strains  
(at the north side of walls)

Response envelopes

Test Model  
(a) Base fixed 50% JMA-Kobe

Test Model  
(b) Base fixed 100% JMA-Kobe

Fig. 11 Local responses of RC walls

249 **5 Discussions of modeling issues**

250 **5.1 Beam-column joint modeling**

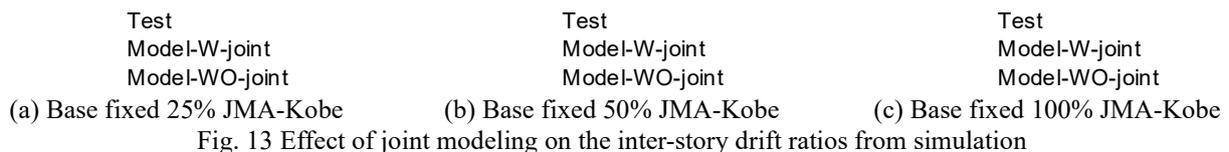
251 Due to insufficient transverse reinforcement, the beam-column joints of the test structure underwent severe damage during

252 the tests. The video records revealed diagonal cracks and slight concrete spalling when subjected to 100% JMA-Kobe in  
 253 base fixed tests (Fig. 12). The scissors model was adopted to incorporate beam-column joints into the numerical model, as  
 254 presented in section 3 (referred to as Model-W-joint in this section). To investigate the effect of beam-column joint  
 255 modeling on the simulation results, another model of the test structure was established for comparison, in which the beam-  
 256 column joints were not modeled, and fiber beams and columns were directly connected at the intersection of their  
 257 centerlines (referred to as Model-WO-joint in this section).



(a) After base fixed 50% JMA-Kobe (b) After base fixed 100% JMA-Kobe  
 Fig. 12 Damage states of a beam-column joint of the 5<sup>th</sup> floor

258 Fig. 13 compares the maximum inter-story drift ratios in the frame direction estimated by the Model-W-joint and Model-  
 259 WO-joint models. This demonstrates that when subjected to 25% and 50% JMA-Kobe (base fixed), there was no obvious  
 260 difference between the results from Model-W-joint and Model-WO-joint, as the beam-to-column joints did not sustain  
 261 significant damage under those shakings. Under base fixed 100% JMA-Kobe, significant drifts (2.6% to 2.9% drift ratio)  
 262 occurred in the 3<sup>rd</sup> to 5<sup>th</sup> stories, but were evidently underestimated by Model-WO-joint. When applying the scissors  
 263 model to represent the joint nonlinear behavior, the Model-W-joint exhibited improved accuracy in simulating the large inter-  
 264 story drift of the 3<sup>rd</sup> to 5<sup>th</sup> stories. The simulation error of the maximum inter-story drift ratio in the 4<sup>th</sup> story decreased from  
 265 19.6% to 4.8% when considering the beam-to-column joint model.



266 The calculated shear deformations of beam-to-column joint zones were further compared with the test data. As shown in  
 267 Fig. 14, shear deformations of the joints on the 2<sup>nd</sup> to 5<sup>th</sup> and 7<sup>th</sup> floors were measured by inclined LVDTs. Fig. 15 indicates  
 268 that the Model-W-joint effectively captured the joint deformations under 25% and 50% JMA-Kobe. When subjected to  
 269 100% JMA-Kobe, significant joint deformations developed. Although the joint model provided an accurate estimate of the

270 shear deformation of the joints of the 2<sup>nd</sup> and 3<sup>rd</sup> floors (i.e., JNT1 and JNT2 in Fig. 14), it overestimated the deformation  
271 of the joints of the 4<sup>th</sup> and 5<sup>th</sup> floors (i.e., JNT3 and JNT4) and underestimated the deformation of the joint of the 7<sup>th</sup> floor  
272 (i.e., JNT6). This discrepancy local joint deformation is consistent with the estimated results of the global inter-story drift  
273 presented in Fig. 13c. The errors are suspicious to be related to the determination of parameter values of the scissors model,  
274 thus indicating a need for improvement of the scissors model in future.

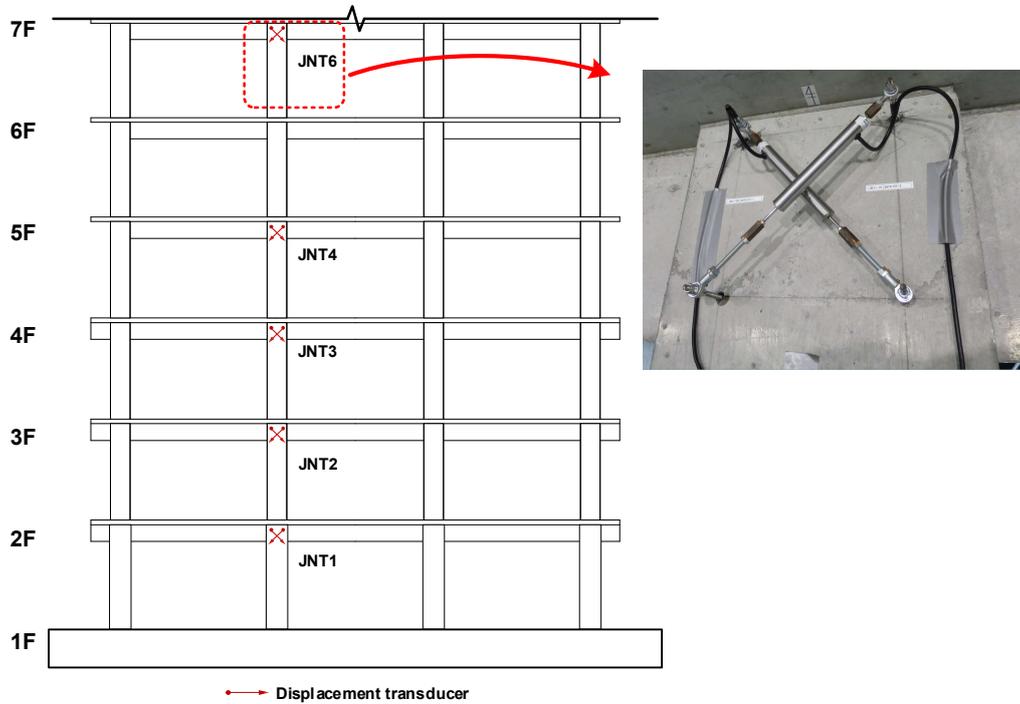
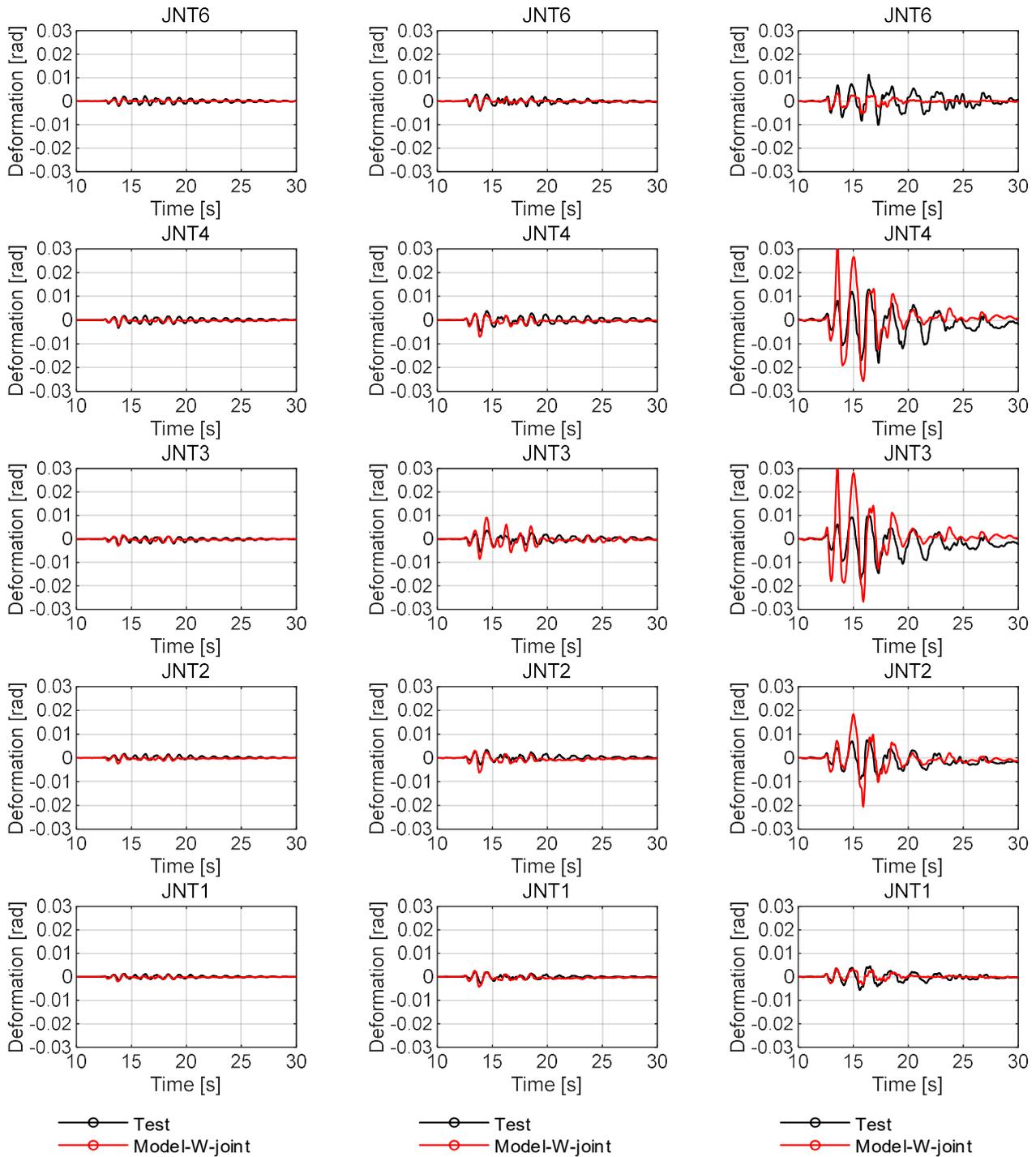


Fig. 14 Measurement of joint deformations



(a) Base fixed 25% JMA-Kobe

(b) Base fixed 50% JMA-Kobe

(c) Base fixed 100% JMA-Kobe

Fig. 15 Joint deformations from experimental and numerical results

275 **5.2 Damping modeling**

276 Classical damping (such as Rayleigh damping) is appropriate if similar damping mechanisms are distributed throughout  
 277 the structure, and the Rayleigh damping model has been widely adopted in structural nonlinear analysis due to its simplicity.  
 278 However, structural damping may be significantly amplified to an unrealistic state when Rayleigh damping is formulated

279 by the structural initial stiffness matrix (Charney 2008, Jehel et al. 2014). Therefore, a “transient” Rayleigh damping model  
 280 was adopted (as illustrated in section 3.3, referred to as Model-T-damping in this section) for the simulation.

281 To quantify the effect of damping modeling on the structural responses from simulation, another structural model with  
 282 “initial” Rayleigh damping was established (referred to as Model-I-damping in this section), where the initial stiffness  
 283 matrix was utilized to construct the Rayleigh damping. Rayleigh proportionality coefficients were determined by modal  
 284 damping ratios and modal frequencies. In both models, a damping ratio of 0.025 was set for the 1<sup>st</sup> and 9<sup>th</sup> structural mode  
 285 and assumed to be constant during the tests, and the modal frequencies for damping formulation were updated after each  
 286 shaking by system identification, which also updated the Rayleigh proportionality coefficients.

287 Fig. 16 compares the inter-story drifts from the Model-T-damping and Model-I-damping against test data. Under base fixed  
 288 50% JMA-Kobe shaking, both models had similar estimation of the inter-story drifts. However, a notable difference was  
 289 observed for the fixed 100% JMA-Kobe loading case, when the structure underwent significant nonlinearity. Particularly  
 290 for the wall direction, a notable improvement in simulation accuracy for the model using “transient” Rayleigh damping  
 291 can be observed, relative to “initial” Rayleigh damping. Therefore, the modeling approach of Rayleigh damping has a non-  
 292 negligible influence on the structural responses, and transient Rayleigh damping is recommended for use in numerical  
 293 modeling.

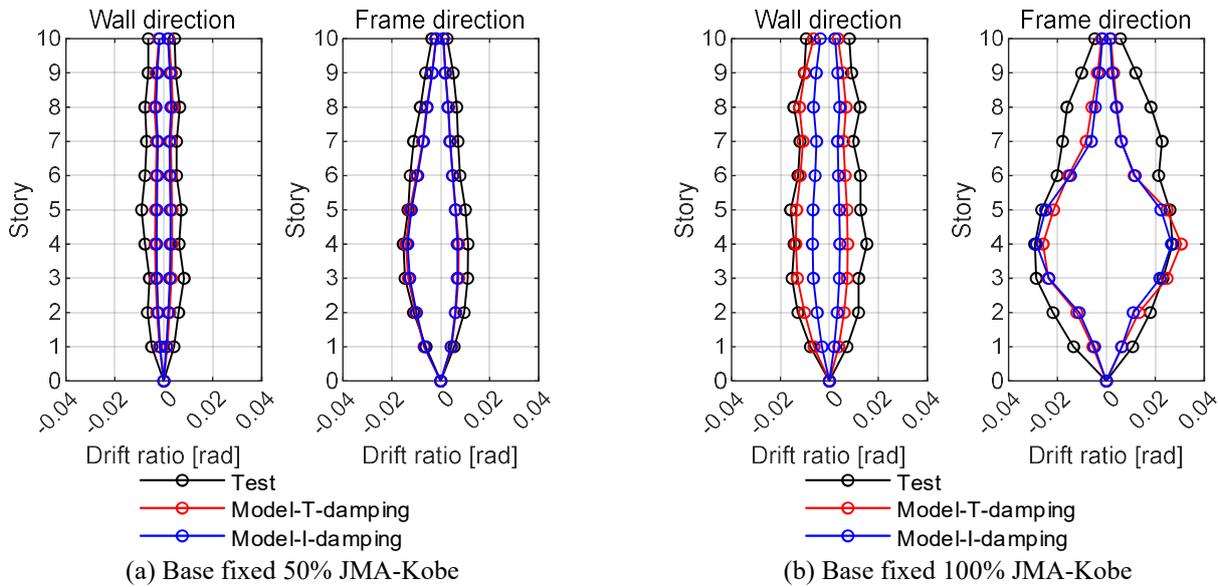


Fig. 16 Effect of damping modeling on the inter-story drift ratios from simulation

## 294 6 Conclusions

295 Shaking table tests of a full-scale ten-story RC building structure conducted at E-Defense provided a unique benchmark  
 296 case for validation of state-of-the-art numerical modeling of RC structures. In this study, a numerical model of the test  
 297 structure was established in OpenSees, which adopted a fiber-based beam-column element for RC beams/columns, multi-  
 298 layer shell element for RC walls, and scissors model for beam-to-column joints. The simulation results were compared  
 299 against test data to assess the ability of the numerical model to capture the structural nonlinear dynamic responses. Based  
 300 on the results, the following conclusions can be drawn.

301 (1) The numerical model provided reasonable simulations of observed global responses, including peak inter-story drift  
 302 ratios, floor accelerations, base shear forces and overturning moments of the test structure within a moderate nonlinear  
 303 state (e.g., under 50% JMA-Kobe motion). For 100% JMA-Kobe motion loading, the numerical model could also  
 304 reasonably predict the peak inter-story drift in the wall direction, with an average error of 14.8%. However, a notable

305 discrepancy was observed between the numerical results and test data of the structural responses in the frame direction,  
306 indicating the numerical model is less accurate for the simulation of significant seismic damage and severe nonlinear  
307 response (peak inter-story drift reaching 2.9%).

308 (2) The multi-layer shell element model reasonably predicted the flexural and shear deformations of RC walls in the bottom  
309 three stories. The average boundary vertical strains of RC walls estimated by the numerical model also matched well with  
310 the measured test data, except for a discrepancy at the wall's bottom vertical tensile strain because the measured data was  
311 influenced by the wall-foundation beam interface cracks.

312 (3) When subjected to 100% JMA-Kobe, the beam-to-column joints of the 4<sup>th</sup> to 6<sup>th</sup> floors were significantly damaged. The  
313 numerical model without beam-column joint modeling underestimated the inter-story drift ratios of the 3<sup>rd</sup> to 5<sup>th</sup> stories.  
314 By incorporating the scissors model to represent the nonlinear behavior of the beam-column joints, the numerical model  
315 provided an improved estimate of the inter-story drifts of stories where the beam-to-column joints experienced severe  
316 damage. Nevertheless, the calculated shear deformations of beam-to-column joint zones had non-negligible discrepancy  
317 with the experimental test data, indicating the necessity for further improvement of beam-to-column joint modeling.

318 (4) The modeling approach of Rayleigh damping has a non-negligible influence on the structural nonlinear responses. A  
319 tangent stiffness matrix is recommended to formulate a system damping matrix, and Rayleigh proportionality coefficients  
320 should be updated after each seismic loading to reflect the effect of a decrease in frequency.

## 321 **Acknowledgements**

322 The authors appreciate the National Research Institute for Earth Science and Disaster Resilience (NIED) for providing the  
323 E-Defense shaking table test data of the 10-story RC building structure. The first three authors are sponsored by the fund  
324 from the National Natural Science Foundation of China (Grant No. 52078277), and they are sincerely grateful to the sponsor.

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420 University of California, Berkeley

#### 421 **Statements and Declarations**

422 **Funding:** The first three authors has received research support from the National Natural Science Foundation of China  
423 (Grant No. 52078277).

424 **Competing Interests:** The authors have no relevant financial or non-financial interests to disclose.

425 **Author Contributions:** All authors contributed to the study conception and design. The modeling and analysis were  
426 performed by Lei Sun, Xiaodong Ji and Yuncheng Zhuang. The test and data collection were performed by Koichi Kajiwara,  
427 Jae-Do Kang and Takuya Nagae. The first draft of the manuscript was written by Lei Sun and Xiaodong Ji. All authors  
428 commented on previous versions of the manuscript. All authors read and approved the final manuscript.

429 **Data Availability:** The datasets generated during and/or analyzed during the current study are available from the  
430 corresponding author on reasonable request.